

1. If  $x[n] = 4\left(\frac{1}{4}\right)^n u[n]$  and  $h[n] = 8\delta[n] + 2\delta[n-1]$ , find  $y[n]$  valid for  $n \geq 1$  using the steady-state method.
2. Compute the solutions to Problem 1 using z transforms.
3. Using the method given in the class notes, design an  $M=2$  FIR LP filter that passes low frequencies up to  $\omega_p = \frac{\pi}{4}$  rads/sample, but stops frequencies higher than  $\omega_s = \frac{3\pi}{4}$  rads/sample. Write the z transform of your filter.
4. Prove the efficiency of the above filter using Matlab to plot its gain function in dB for  $\omega=0$  to  $\pi$  rads/sample.