

1. Consider the following finite-length sequences with $N=8$ defined for $0 \leq n \leq 7$:

- $x_1[n] = [1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1]$
- $x_2[n] = [1 \ 1 \ 0 \ 0 \ 0 \ 0 \ -1 \ -1]$
- $x_3[n] = [0 \ 1 \ 1 \ 0 \ 0 \ 0 \ -1 \ -1]$
- $x_4[n] = [0 \ 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1]$

Without explicitly calculating their DFT, answer the following questions:

- a. Which have a purely real DFT (i.e. which are purely pcs?)
 - b. Which have a purely imaginary DFT (i.e. which are purely pca?)
 - c. Which have $X[k=0] = 0$? (Hint: use last homework assignment's answer on what $X[k=0]$ simplifies to).
2. Graphically find this circular convolution: $[6 \ 2 \ 4] \circledast_3 [1 \ 1 \ 1]$ if both sequences are finite length starting at $n=0$.
3. If $x[n] \circledast_5 h[n] = [8 \ 2 \ 9 \ 10 \ -4]$ (and the answer starts at $n=0$ as usual), can you find $x[n] \circledast_4 h[n]$? If so, what is it?
4. To find the **linear** convolution of $x[n] = [1 \ 2 \ 3]$ with $h[n] = [1 \ 1 \ 1 \ 1 \ 1]$ using DFTs, how many zeros must you end-pad x and h by? i.e. in Matlab, how many zeros would you have to end-pad x and h by before evaluating `>> ifft(fft(x) .* fft(h))`
5. If you are only interested in graphing the energy density of a signal (i.e. $|X[k]|^2$) does it make a difference if you zero pad the beginning or the end of the signal? Why?