

P1 Find: Let $g[n]$ be even, $h[n]$ be odd.

a) is $x[n] = g[n] g[n]$ odd or even? Prove.

b) is $y[n] = h[n] h[n]$ odd or even? Prove.

Hints:

- An example is not a proof. A proof works for any function.
- Don't confuse an odd or even *number* with an odd or even *function*.

P2 Find: Using the graphs on the right, for the infinite length sequences a and b, state if they are conjugate symmetric or antisymmetric. For the finite length sequences c-e state if they are periodic conjugate symmetric or periodic conjugate antisymmetric.

P3 Find: a) For the infinite length sequence $x[n] = 2^n$, find the conj symmetric part $x_{cs}[n]$ and the conjugate anti-symmetric part $x_{ca}[n]$. Simplify for full credit.

b) The finite length sequence $y[n] = [\mathbf{1} \ 2 \ 3 \ 4 \ 5]$ where $y[0]$ is bolded, is defined over $0 \leq n \leq 4$. Find the periodic conjugate symmetric part $y_{pcs}[n]$ and the conjugate antisymmetric part $y_{pca}[n]$. Write the result as a sequence using an arrow to identify $n = 0$.

c) Redo (b) but using the finite-length sequence $z[n] = [\mathbf{0} \ 1+j \ 1-j]$, defined over $0 \leq n \leq 2$. Remember to identify $n=0$ with an arrow.

Hints:

- a) the only digits used are 1 and 2
- b) 0.5, 1.5, and 3.5 will feature prominently
- c) does the given sequence $z[n]$ have a symmetry?

P4 Find: Are the following sequences bounded?

a) $x[n] = A\alpha^n$ where A and α are complex and $|\alpha| < 1$

b) $x[n] = A\alpha^n \mathbf{u}[n]$ where A and α are complex and $|\alpha| < 1$
note: $\mathbf{u}[n]$ is a unit step; it is 1 for $n \geq 0$, and 0 otherwise

Hints: for a) consider what happens as n becomes more negative

