

1. What kind of symmetry, if any, does the following signal have? The $n=0$ index is bolded and the sequence is zero outside the area shown.
 $x[n] = [\textbf{8} \quad 2+j \quad -7 \quad 2-j]$

It is finite length, so the only type of symmetry possible is a periodic symmetry. To see if it has any symmetry, first form the periodic extension to the left of $n=0$:

$$[2+j \quad -7 \quad 2-j \quad \textbf{8} \quad 2+j \quad -7 \quad 2-j]$$

(e.g. from $[A \ B \ C \ D]$ to $[B \ C \ D \ A \ B \ C \ D]$)

Next conjugate the elements for $n < 0$

$$[2-j \quad -7 \quad 2+j \quad \textbf{8} \quad 2+j \quad -7 \quad 2-j]$$

Last, ask if the resulting conjugate periodic extension is even (then the original sequence is periodic conjugate symmetric) or odd (the original sequence is periodic conjugate antisymmetric).

It is even, so: periodic conjugate symmetric.

2. In the sequence $x[n]$ given in problem 1, find (using the correct N for the sequence):

a. $x[\langle 3 \rangle_N]$

$N = 4$ for this sequence.

$\langle 3 \rangle_4$ means “add/subtract 4’s from 3 until 3 is in range $0 \leq n < 4$ ” = 3

$$x[\langle 3 \rangle_4] = x[3] = \boxed{2-j}$$

b. $x[\langle 7 \rangle_N]$

$\langle 7 \rangle_4$ means “add/subtract 4’s from 7 until 7 is in range $0 \leq n < 4$ ” = 3

$$x[\langle 7 \rangle_4] = x[3] = \boxed{2-j}$$

c. $x^*[\langle -1 \rangle_N]$

$\langle -1 \rangle_4$ means “add/subtract 4’s from -1 until -1 is in range $0 \leq n < 4$ ” = 3

$$x^*[\langle -1 \rangle_4] = x^*[3] = (2-j)^* = \boxed{2+j}$$