

1. Given continuous time signal  $x(t) = 2 \cos(6t)$  sampled at a sampling frequency of  $f_s$ , evaluate to a number the discrete time signal  $x[n]$  for  $n=0, 1, 2$  if:

a.  $f_s = \frac{2}{\pi} \text{ Hz}$

$$T_s = 1/f_s = \pi / 2 \text{ sec}$$

$$x[n] = x(t = n T_s) = x(\pi n / 2) = 2 \cos(6 \pi n / 2) = 2 \cos(3 \pi n)$$

$$x[0] = 2 \cos(0 \pi) = \boxed{x[0] = 2}$$

$$x[1] = 2 \cos(3 \pi) = 2 \cos(\pi) = \boxed{x[1] = -2} \quad (\text{since adding or subtracting } 2\pi \text{ changes nothing})$$

$$x[2] = 2 \cos(6 \pi) = 2 \cos(0) = \boxed{x[2] = 2}$$

b.  $f_s = \frac{1}{2\pi} \text{ Hz}$

$$T_s = 1/f_s = 2\pi \text{ sec}$$

$$x[n] = x(t = n T_s) = x(2\pi n) = 2 \cos(12 \pi n) = 2 \cos(0) = 2$$

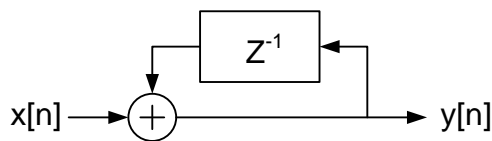
since can add or subtract  $2\pi$  multiples

$$\boxed{x[0] = 2}$$

$$\boxed{x[1] = 2}$$

$$\boxed{x[2] = 2}$$

2. Given discrete time signal  $x[n] = \begin{cases} 0, & n < 0 \\ 1, & n \geq 0 \end{cases}$  and the system below, find  $y[n]$  for  $n=0, 1, 2$ , and 3.



for  $n < 0$ ,  $x[n]$  is always 0 so  $y[n]$  and the output of  $z^{-1}$  (i.e.  $y[n-1]$ ) is also 0.

for each  $n \geq 0$ , evaluate  $x[n]$  first, then the output of  $z^{-1}$  (which is  $y[n-1]$ ), then add to find  $y[n]$ , so

$n=0$ :  $x[n] = 1$ . The output of  $z^{-1} = y[-1] = 0$  from above. The sum =  $1+0 = \boxed{y[0] = 1}$

$n=1$ :  $x[n] = 1$ . The output of  $z^{-1} = y[0] = 1$  from above. The sum =  $1+1 = \boxed{y[1] = 2}$

$n=2$ :  $x[n] = 1$ . The output of  $z^{-1} = y[1] = 2$  from above. The sum =  $1+2 = \boxed{y[2] = 3}$

$n=3$ :  $x[n] = 1$ . The output of  $z^{-1} = y[2] = 3$  from above. The sum =  $1+3 = \boxed{y[3] = 4}$