

Given: $f(t)$ shown to the right

Find: The Fourier Transform $F(\omega)$ using the integral definition. Express in cos form.

$$\begin{aligned}
 F(\omega) &= \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt \\
 &= \int_{-\infty}^{\infty} [2\delta(t-1) + 2\delta(t+1)] e^{-j\omega t} dt \\
 &= 2(e^{j\omega} + e^{-j\omega}) \text{ from sketch} \\
 &= 4 \left[\frac{1}{2} (e^{j\omega} + e^{-j\omega}) \right] \\
 &= \boxed{4 \cos(\omega)}
 \end{aligned}$$

