

P1 Use Laplace Transforms to find $i(t)$.

Note: NOT $I(s)$ but $i(t)$.

$$\frac{1}{s} \quad \begin{array}{c} \text{---} \text{---} \text{---} \\ | \\ \text{---} \text{---} \text{---} \\ | \\ s \end{array} \Rightarrow I(s) = \frac{V(s)}{Z(s)}$$

$$I(s) = \frac{\frac{1}{s}}{1 + \frac{1}{s} + s} = \frac{1}{s^2 + s + 1} \quad \text{poles } s = \frac{-1 \pm \sqrt{1-4}}{2}$$

$$= \frac{-1 \pm j\sqrt{3}}{2} = -\frac{1}{2} \pm j\frac{\sqrt{3}}{2} = 0.5 \pm j0.866$$

$$= \frac{1}{(s + \frac{1}{2} - j\frac{\sqrt{3}}{2})(s + \frac{1}{2} + j\frac{\sqrt{3}}{2})}$$

$$= \frac{A}{s + \frac{1}{2} - j\frac{\sqrt{3}}{2}} + \frac{A^*}{s + \frac{1}{2} + j\frac{\sqrt{3}}{2}} \quad A = \frac{1}{(-\frac{1}{2} + j\frac{\sqrt{3}}{2}) + \frac{1}{2} + j\frac{\sqrt{3}}{2}} = \frac{1}{j\sqrt{3}} = \frac{0.577}{\angle -90^\circ}$$

$$\times 2 = 1.15$$

$$i(t) = 1.15 e^{-\frac{1}{2}t} \cos(0.866t - 90^\circ) \text{ A}$$

