

Solving First-Order Circuits

EE223

First, ask: is it a first order circuit? It needs (1C or 1L) and at least 1R, usually more, and something that causes a change - a switch or a $v(t)$ or $i(t)$ source. Then:

- ① Draw $t < 0$ to find I_{C0} or I_{L0} NO MATTER WHAT YOU ARE ASKED TO FIND!!
In this DC steady state region

$\frac{1}{s} \Rightarrow \begin{matrix} \circ + \\ \\ \circ - \end{matrix} \Rightarrow I_{C0}$	$\{ \Rightarrow \downarrow I_{L0}$	switches $\Rightarrow$ opens or shorts	$v(t) \Rightarrow$ evaluate ex: $2v(t) + 3 \Rightarrow 3$
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- ★ ② Draw $t \geq 0$ to find R_{Th} seen by C or L , then find τ
To find R_{Th}

$\oplus \Rightarrow$ short	$\oplus \Rightarrow$ open	switches $\Rightarrow$ opens or shorts	$v(t) \Rightarrow$ evaluate ex: $2v(t) + 3 \Rightarrow 5$
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- ③ Draw $t = \infty$ to find $I_{C\infty}$ or $I_{L\infty}$ NO MATTER WHAT YOU ARE ASKED TO FIND!!

same substitutions as in ① DC steady state except the example
 $2v(t) + 3$ would evaluate to 5

④
$$v_C(t) = \begin{cases} I_{C0} \\ I_{C\infty} + (I_{C0} - I_{C\infty})e^{-t/\tau} \end{cases}, \begin{matrix} t < 0 \\ t \geq 0 \end{matrix} \quad \tau = RC$$

$$i_L(t) = \begin{cases} I_{L0} \\ I_{L\infty} + (I_{L0} - I_{L\infty})e^{-t/\tau} \end{cases}, \begin{matrix} t < 0 \\ t \geq 0 \end{matrix} \quad \tau = L/R$$

- ⑤ Find whatever asked to find. Ex: $i_C(t) = C v_C'(t)$
 $v_L(t) = L i_L'(t)$
also can use Ohm's Law, KVL, KCL

- ★ If there is an opamp, follow step ② but also replace the C or L with a $1A \oplus \downarrow v_T$ or a $1V \oplus \uparrow i_T$ and find the resulting v_T

or i_T for the test current or voltage source respectively. Then
 $R_{Th} = \frac{v_T}{1A}$ for the test current or $R_{Th} = \frac{1V}{i_T}$ for the test voltage.

-COL Squire