

1. Find the derivatives of the following functions:

a. $v(t) = 2t^2 + 8t + 9$ $\boxed{4t + 8}$

b. $i(t) = \frac{2}{3}e^{-2t}$ $\frac{2}{3}(-2)e^{-2t} = \boxed{-\frac{4}{3}e^{-2t}}$

c. $q(t) = 2k \cos(12t)$ $\boxed{-2k \cdot 12 \sin(12t) = -24k \sin(12t)}$

d. $v(t) = 3e^{-2t} \cos(6t + \frac{\pi}{4})$ $3 \left[e^{-2t} \frac{d}{dt} \left\{ \cos(6t + \frac{\pi}{4}) \right\} + \frac{d}{dt} \{ e^{-2t} \} \cos(6t + \frac{\pi}{4}) \right]$
 $= \boxed{-18e^{-2t} \sin(6t + \frac{\pi}{4}) - 6e^{-2t} \cos(6t + \frac{\pi}{4})}$

2. Find the integrals of the following functions:

a. $v(t) = \int_0^2 6 dt = 6t \Big|_0^2 = \boxed{12}$

b. $q(t) = \int_0^t 9\tau^2 + \tau d\tau = 3\tau^3 + \frac{1}{2}\tau^2 \Big|_0^t = \boxed{3t^3 + \frac{1}{2}t^2}$

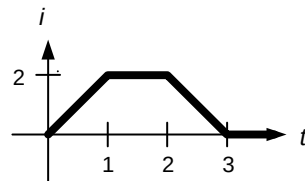
c. $i(t) = \int_{-\infty}^2 3e^{4t} dt = \frac{3}{4}e^{4t} \Big|_{-\infty}^2 = \frac{3}{4} \left[e^8 - e^{-\infty} \right] = \boxed{\frac{3}{4}e^8} \approx 2236$

d. $\omega(t) = \int_t^\infty p(\tau) d\tau$ if $p(t) = e^{-2t} = -\frac{1}{2}e^{-2\tau} \Big|_t^\infty = \boxed{\frac{1}{2}e^{-2t}}$

e. $\omega(t) = \int_{-\infty}^t p(\tau) d\tau$ if $p(t) = t$ for $t \geq 0$ and $\omega(0) = 2$. Only solve for $t \geq 0$.
 $= \int_{-\infty}^0 p(\tau) d\tau + \int_0^t p(\tau) d\tau = \omega(0) + \int_0^t \tau d\tau = 2 + \frac{1}{2}\tau^2 \Big|_0^t = \boxed{2 + \frac{1}{2}t^2}$

f. $q(t) = \int_0^{\pi/4} 3 \cos(2t) dt = \frac{3}{2} \left[\sin \frac{\pi}{2} - \sin 0 \right] = \boxed{\frac{3}{2}}$

3. Find $q(t) = \int_{-\infty}^t i(\tau) d\tau$ for $t \geq 0$ if $q(0) = 2$ and $i(t) =$



t region	i(t)	t ₀	q(t ₀)	$\int_{t_0}^t i(\tau) d\tau + q(t_0)$
$0 \leq t < 1$	$2t$	0	2	$\int_0^t 2\tau d\tau + 2 = t^2 + 2$
$1 \leq t < 2$	2	1	$t^2 + 2 \Big _1 = 3$	$\int_1^t 2 d\tau + 3 = 2t + 1$
$2 \leq t < 3$	$-2(t-3)$	2	$2(2) + 1 = 5$	$\int_2^t -2(\tau-3) d\tau + 5 = -t^2 + 6t - 3$
$t \geq 3$	0	3	$-3^2 + 6(3) - 3 = 6$	$\int_3^t 0 d\tau + 6 = 6$

$$q(t) = \begin{cases} t^2 + 2, & 0 \leq t < 1 \\ 2t + 1, & 1 \leq t < 2 \\ -t^2 + 6t - 3, & 2 \leq t < 3 \\ 6, & t \geq 3 \end{cases}$$